

Review 10 optimization

candidate list 1. endpoints

critical points $\begin{cases} 2. f' = 0 \\ 3. f' \text{ undefined} \end{cases}$

absolute extrema: (there can only be one)

plug candidates into $f(x)$, choose most extreme value

relative extrema (could be more than one)

1st der test $+0-$, $-0+$ sentence

2nd der test $f' = 0$ $f'' < 0$ (max) $f'' > 0$ (min)

⚠ "is" vs "at"

$y = -15$ max max at $x = -$

Feb 28-12:40 PM

Ex 1. Storm washes sand away from a beach causing the water to get closer to a road. The storm lasts 5 hours. Water gets closer to the road at a rate of $f(t) = \sqrt{t} + \cos t - 3$. When is distance from water to road dec. most rapidly?

$$f'(t) = \frac{1}{2\sqrt{t}} - \sin t = 0$$

candidates $t=0$ $f(0) = -2$

$t=5$ $f(5) = -0.4803$

when $t = 2.8404$, $f(2.8404) = -2.2697$

$t = 0.6619$ $f(0.6619) = -1.3976$

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Review 10 optimization

candidate list 1. endpoints

2. $f' = 0$

3. f' undefined

absolute extrema: plug candidates into $f(x)$

relative extrema:

1st der test $+0-$ or $-0+$, sentence

2nd der test $f' = 0$ $f'' < 0$ (max) $f'' > 0$ (min)

⚠ "is" vs "at"

y x

Feb 28-1:10 PM

Ex 1. A storm washes sand away from a beach causing the water to get closer to a road

at a rate of $f(t) = \sqrt{t} + \cos t - 3$ $\frac{ft}{hr}$

The storm lasts 5 hours. When is the distance from the water to the road decreasing most rapidly?

$$f'(t) = \frac{1}{2\sqrt{t}} - \sin t = 0$$

$t=0$ $f = -2$

$t=5$ $f = -0.4803$

when $t = 2.8404$ hr

$t = 0.6619$ $f = -1.3976$

$t = 2.8404$ $f = -2.2697$ $\frac{ft}{hr}$

Feb 28-1:26 PM